Car ownership and the Labor Market of Ethnic Minorities*

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Abstract

We show how initial wealth differences between low-skilled minority and white workers can generate differences in their labor-market outcomes. This even occurs in the absence of a taste for discrimination against ethnic minorities or exogenous differences in the distance to jobs. Because of the initial wealth difference, minorities cannot afford to buy a car while whites can. Car ownership allows whites to reach more jobs per unit of time, which gives them a better bargaining position in the labor market. As a result, in equilibrium, ethnic minorities end up with both higher unemployment rates and lower wages than whites. Furthermore, we also show that it takes more time for minorities to reach their jobs even though they travel less miles when they are employed. Those predictions are consistent with the data. Better access to capital markets or better public transportation will reduce the differences in labor market outcomes.

Key words: Transportation mismatch, job search, spatial labor markets, multiple job centers, ethnic minorities.

JEL Classification: D83, J15, J64, R1.

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Urban transit systems in most American cities . . . have become a genuine civil rights issue-and a valid one-because the layout of rapid-transit systems determines the accessibility of jobs to the Black community. If transportation systems in American cities could be laid out so as to provide an opportunity for poor people to get meaningful employment, then they could begin to move into the mainstream of American life. A good example of this problem is my home city of Atlanta, where the rapid-transit system has been laid out for the convenience of the white upper-middle-class suburbanites who commute to their jobs downtown. The system has virtually no consideration for connecting the poor people with their jobs.

Martin Luther King, Jr. (1986, pp. 325-326)

1 Introduction

Empirical evidence for the United States suggests that, relative to white workers, African American workers: (i) are less likely to own a car, (ii) experience higher unemployment rates and longer unemployment spells, (iii) earn lower wages, (iv) spend more time commuting to work, (v) travel less miles to go to their jobs, (vi) search for jobs in a smaller area. See e.g. Holzer et al. (1994) and Raphael and Stoll (2001). Many papers, some of which are discussed below, offer explanations for a subset of those facts. The aim of this paper is to construct a model that can simultaneously explain all of them.

Most of the literature has focussed on why ethnic minorities1 experience higher unemployment rates and earn lower wages than whites. Different answers have been given to those crucial questions but the recent debate, especially in the United States, has been focusing on the role of segregation in explaining these unemployment rate differences. The spatial mismatch hypothesis, first formulated by Kain (1968), states that, residing in urban segregated areas distant from and poorly connected to major centers of employment growth, African American workers2 face strong geographic barriers to finding and keeping well-paid jobs. In the U.S. context, where jobs have been decentralized and African Americans have stayed in the central part of cities, the main conclusion of the spatial mismatch hypothesis is to put forward the distance to jobs as the main culprit for the high unemployment rates among blacks.

Since the study of Kain, dozens of empirical studies have been carried out trying to test

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1The term “ethnic minority” refers to any “visible minority”. This would include African Americans and Hispanics in the United States, Indians and Pakistanis in the UK, Turks in Germany, North Africans in France, etc.

2The recent debate on the spatial mismatch hypothesis in the US has also included Hispanic workers.
this hypothesis. The usual approach is to relate a measure of labor-market outcomes, based on either individual or aggregate data, to another measure of job access, typically some index that captures the distance from residences to centers of employment. The bulk of the evidence suggests that bad job access indeed worsens labor-market outcomes, confirming the spatial mismatch hypothesis (for literature surveys, see Ihlanfeldt and Sjoquist, 1998; Gobillon et al., 2005; Ihlanfeldt, 2006; Zenou, 2009).

However, spatial mismatch cannot explain all the facts described above. In particular, it cannot explain why minority workers travel less miles to work but why it takes more time for them. It is therefore important to introduce mode choices in the explanation. Some researchers have even put forward the idea of an automobile or transportation mismatch rather than a spatial mismatch to understand the adverse labor-market outcomes of black workers in the United States (see, in particular, Taylor and Ong, 1995). Since most minority use mass transit, the choice of transportation is indeed crucial, in particular, in large American metropolitan areas where public transportation is not that good (see e.g. Pugh, 1998). Indeed, mass transit is a much slower transport mean than private cars in the United States not only because buses are slower but also because of the unreliability of the transit system.

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3Theoretical models that explicitly model the spatial aspects of the labor market (see, in particular, Coulson et al., 2001; Brueckner and Zenou, 2003; Smith and Zenou, 2003; Sato, 2001, 2004) have mainly tried to explain the spatial mismatch hypothesis thus focussing on distance to jobs as the main culprit for the adverse labor-market outcomes of black workers (for an overview, see Zenou, 2009). There are also some search models that study how workers determine their maximum area of search (see e.g. Schwartz, 1976 or Seater, 1979) but neither mode choice nor race are introduced in their models. To the best of our knowledge, our paper is the first that develops a search-matching model where mode-choice decisions affect labor-market outcomes of minority and white workers.

4Using data drawn from the 1995 Nationwide Personal Transportation Survey, Raphael and Stoll (2001) show that, in the US, 5.4 percent of white households have no automobile while 24 and 12 percent of respectively the black and Latino households do not own a car. Even more striking is that they show that respectively 64 and 46 percent of black and Latino households have only one or zero cars whereas this number was 36 percent for white households. In Great-Britain, using the 1991 Census data, Owen and Green (2000) show that people from minority ethnic groups are more than twice as likely as white people to depend on public transport for commuting journeys (33.2 versus 13.7 percent), with nearly three-fifths of Black-African workers using public transport to go to work. Furthermore, 73.6 percent of the whites use a private vehicle while this number is only 56.4 percent for ethnic minorities (and 39.6 percent for Black-African workers). Using the Labour Force Survey for England, Patacchini and Zenou (2005) find similar results.

5In U.S. Metropolitan Statistical Areas, the lack of good public transportation is a real problem. For instance, the New York Times of May 26, 1998, was telling the story of Dorothy Johnson, a Detroit inner-city black female resident who had to commute to an evening job as a cleaning lady in a suburban office. By using public transportation, it took her two hours whereas, if she could afford a car, the commute would have taken only 25 minutes.
that causes workers to frequently miss transfers and of the fact that many areas are difficult to reach by public transport. In the United States, in 2000, the average commuting time by public transit was about twice as high as by car (47.7 versus 24.1 minutes; see Kawabata and Shen, 2007). As a result, some jobs will be turned down by ethnic minorities, not because these jobs are too far away but because they are difficult to access. So our main point here is that car access can have an negative impact on the labor-market of minority workers. In particular, because of urban sprawl and increasing job creation in the suburbs in the United States (Brueckner, 2000, 2001; Glaeser and Kahn, 2001; Glaeser and Shapiro, 2003; Glaeser and Kahn, 2004; Nechyba and Walsh, 2004), minority families, who mostly reside in the central part of cities, are more and more isolated from jobs that potentially match their skills (Wassmer, 2008).6 Given this sprawling, access to good transportation enables residents to conduct geographically broader job-search, accept offers further away from home, improve work attendance, and keep the commute burden to a reasonable level. In other words, in the highly auto-oriented US metropolitan areas, the number of accessible job opportunities is considerably lower for public transit users than for car users (Hess, 2005; Shen, 1998). It is then reasonable to hypothesize that car ownership is an important factor in improving the employment status of low-skilled minority workers. In our model, we show that not having access to cars has a dramatic impact on their labor market outcomes.

It is well-known that taste discrimination and distance to jobs can explain the adverse labor-market outcomes of minority workers (see, for example, the spatial-mismatch literature discussed above). In this paper, we want to show that, even if these aspects are not taken into account, car access will still lead to substantial differences between minority and white workers. Both job and car access are certainly important in explaining these differences and only an empirical test can give an answer to this question. Interestingly, Patacchini and Zenou (2005) show that distance to jobs and car access account for almost the same percentage (23.86 and 26.45 respectively) of the disparity between whites’ and nonwhites’ search intensities in the UK.

Let us now explain the model. As stated above, firms have no taste for discrimination and ex ante ethnic minorities and whites are located at the same distance to jobs. Apart from the color of their skin, the only difference between minorities and whites is an initial wealth difference.7 We show that this forces minority workers to choose public transportation while

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6In the United States, between 1970 and 1990, the ratio of jobs to workers in the central city declined from 1.2 to 1 for whites, while for blacks the ratio declined to 0.7 (O’Regan and Quigley, 1998). This indicates that a sizable fraction of minority workers are reverse commuters, that is, they live in central cities and work in the suburban ring.

7The wealth difference between African Americans and whites, and between Hispanics and whites in the
whites can afford cars. Since the set of jobs that can be reached by car is larger than the set that can be reached by public transportation, whites find jobs faster and experience shorter unemployment spells. Living far away from one’s job could in principle signal car ownership but not if home location is either unobservable or not verifiable (i.e. workers can always provide fake addresses). Employers do observe the worker’s type (minority or white) and since whites have on average a better bargaining position, they earn higher wages. This is a standard statistical discrimination argument (see e.g. Arrow, 1973 or Phelps, 1972).

So, the main idea behind our results is that the set of available jobs for minority workers who mainly use public transportation is smaller than for whites who can travel much faster. In other words, ethnic minorities will refuse some jobs that are not accessible by public transportation while they would have accepted them if they had a car.8 Zax and Kain (1996) have illustrated this issue by studying an interesting “natural experiment” (the case of a large firm in the service industry that relocated from the center of Detroit to the suburb Dearborn in 1974).9 Among workers whose commuting time was increased, black workers were over-represented, and not all of them could follow the firm. This had two consequences. First, segregation forced some African Americans to quit their jobs. Second, the share of black workers applying for jobs to the firm drastically decreased (53% to 25% in 5 years before and after the relocation), and the share of black workers in hires also fell from 39% to 27%.10 This highlights the fact that African American workers may refuse jobs that involve too long commutes, not necessarily because they are far away in terms of miles traveled but because they are not reachable by public transportation.

The paper is organized as follows. In section 2, we discuss the model and its assumptions. Section 3 characterizes the equilibrium and derives the sources of differences in labor market outcomes between blacks and whites. Section 4 discusses some policy implications of the model.

8 Using data from the European Community Household Panel (ECHP) for 1994-2001 and for a sample of currently unemployed job seekers, Rupert et al. (2009) report that 14.7% of job offers were turned down due to commute distance. They also indicate that the impact of commute distance is roughly a third lower than the impact of the wage rate when the job acceptance decision has to be made.

9See also Fernandez (1994) for a similar “natural experiment”.

10 For a survey on these issues, see Fernandez and Su (2004).
2 The model

2.1 Labor market flows

We consider a continuum of workers and firms. The total mass of workers is normalized to one. A fraction \((1 - p)\) of the workers are from the ethnic minority group and a fraction \(p\) are whites. Both are assumed to be identical apart from the color of their skin and a difference in initial wealth. We assume that whites have higher wealth flows than ethnic minorities, i.e. \(\Omega_W > \Omega_B\), where the subscript \(k = B, W\) denotes the type of an individual. Differences in initial wealth can be justified on the ground that minorities and whites did not experience the same history. For example, in the United States, Smith (1995) documents that racial and ethnic wealth disparities are large. These minority wealth disparities are due in part to differential inheritances and desired bequests as inequities perpetuate themselves across generations; the disparities are also due to lower minority incomes, poorer health.\(^{11}\) We can also interpret the difference between \(\Omega_W\) and \(\Omega_B\) in terms of access to the capital market. It is well-documented that, in the United States, black families have a more difficult access to the capital market. Indeed, they pay higher interest rates on the loans used to purchase housing (Charles and Hurst, 2002; Mayer et al., 2008) and vehicles (Cohen, 2007; Charles et al., 2008). For example, Cohen (2007) finds that roughly 43% to 72% of blacks are charged interest rate “markups” while only 22% to 47% of whites face these higher prices for vehicle financing. Charles et al. (2008) show that the interest rates for vehicle loans paid by blacks are, on average, a full 100 basis points higher: 10.6% versus 9.6%.

Following Salop (1979), we model workers’ and firms’ heterogeneity by means of a circle along which workers are uniformly distributed over its circumference \(C\) of length 1.\(^{12}\) This is the geographical space and we denote by \(0 \leq x_{ij} \leq 1/2\) the geographical distance between a worker located in \(i\) and a firm located in \(j\).\(^{13}\) It is assumed that workers are unable to change their residential location. One way to justify this assumption is that homes are less mobile than jobs (Manning, 2003).

Time is continuous and workers live forever. At each moment in time, a worker can be

\(^{11}\)This is a well-documented fact (see, e.g. Barsky et al., 2002). Because wealth is usually transferred from generation to generation, the large current racial wealth gap between African Americans and whites may be a function of past racial differences in economic conditions and opportunities (due to the very specific history of African Americans, that is slavery).

\(^{12}\)See, among others, Helsley and Strange (1990), Marimon and Zilibotti (1999), Hamilton et al. (2000), Brueckner et al. (2002), Gautier et al. (2008) for a similar way of modelling heterogeneity.

\(^{13}\)Because it is a circle of length 1 where distance is measured on both sides, the maximum distance between a firm and a worker is 1/2.
either employed or unemployed. All unemployed workers search for a job and we assume that there is no on-the-job search. Similarly, at each moment in time, a firm can have either a filled position or an open vacancy. Let \( u_k(i) \) be the number of type \(-k\) unemployed workers, \( k = \{B, W\} \), (or equivalently the unemployment rate of type \( k \)-workers) at location \( i \) and \( v(j) \) the number of vacancies (or equivalently the vacancy rate) at location \( j \).

The uniform distribution of workers over the circle implies that \( u_k(i) = u_k, \forall i \in C \). It is easy to show (see Lemma 1 of Marimon and Zilibotti, 1999) that, in this case, there exists a stationary equilibrium with a uniform distribution of vacancies at all locations, i.e. \( v(j) = v \), for all \( j \in C \). Gautier et al. (2006, 2009) show that this distribution must be unique. The intuition for this result is that if this distribution is non-uniform than there exists a profitable deviation for firms in non-dense areas (in terms of workers), namely to move to a denser area.

In standard search-matching models, individuals choose reservation wages by comparing the values of employment and unemployment and equating them at the margin.\(^{14}\) In the present model, we include space into a search-matching model and this creates a new decision for job seekers and firms. Workers must now also decide how large the area of search is and firms where to locate, given the location of workers.

To be more precise, search is random and the number of contacts between workers and firms is given by:

\[
M(u_B + u_W, v) \equiv M.
\]

As usual (Pissarides, 2000), \( M(.) \) is assumed to be increasing in its arguments, concave and exhibits constant returns to scale. Let \( \theta = v / (u_B + u_W) \) be labor-market tightness. The contact rate for type \( k \) workers with a vacancy is given by:

\[
\frac{M}{u_B + u_W} \equiv m(\theta)
\]

The contact rate of a vacancy with a type \(-k\) worker is given by:

\[
\frac{M u_k}{v (u_B + u_W)} = \frac{u_k}{u_B + u_W} \frac{m(\theta)}{\theta}
\]

By using the properties of the matching function, it is easy to see that

\[
m'(\theta) > 0 \quad \text{and} \quad \frac{\partial [m(\theta)/\theta]}{\partial \theta} < 0
\]

since more vacancies increase the rate at which workers find a job and decrease the rate at which firms fill a vacancy. We also assume the standard Inada conditions on \( M(.) \), which ensure that \( \lim_{\theta \to +\infty} m(\theta) = \lim_{\theta \to 0} m(\theta)/\theta = +\infty \), \( \lim_{\theta \to 0} m(\theta) = \lim_{\theta \to +\infty} m(\theta)/\theta = 0 \).

\(^{14}\)See e.g. Diamond (1982), Mortensen (1982), Pissarides (2000).
We can now model precisely the matching process between a worker of type $k$ and a firm. For a worker, a match will occur if and only if:

$$\text{Match}_{u_k \rightarrow v} = \frac{m(\theta)}{2\widehat{x}_k} \times \text{Random contact} \times \text{Probability contact is acceptable}$$

where “$\text{Match}_{u_k \rightarrow v}$” means a match between an unemployed worker of type $k$ and firm with a vacancy $v$. Indeed, a match is the product of a random contact rate $m(\theta)$ and an acceptance rule $2\widehat{x}_k$. Independently of race, job contacts arrive randomly to workers at rate $m(\theta)$ (for example, workers read newspapers and observe advertisements). For a given job contact, workers must decide to apply or not to this job, depending on its location. This second stage depends on the chosen transport mode. Observe that the term $\widehat{x}_k$ is multiplied by 2 because each worker considers the distance to jobs from both sides of his/her location.

The rate at which vacancies match with a type $-k$ worker is given by:

$$\text{Match}_{v \rightarrow u_k} = \frac{u_k}{u_B + u_W} \frac{m(\theta)}{\theta} \times \text{Random contact} \times \text{Probability contact is acceptable}$$

where “$\text{Match}_{v \rightarrow u_k}$” means a match between a firm with a vacancy $v$ and an unemployed worker of type $k$. The main difference between “$\text{Match}_{u_k \rightarrow v}$” and “$\text{Match}_{v \rightarrow u_k}$” is that, in the former, we take the viewpoint of a worker while, in the latter, we focus on the firm matching process. First, firms advertise their jobs. They are then contacted by workers and will offer a job only to type $-k$ workers located within a distance $x \leq \widehat{x}_k$.

We assume that jobs are destroyed at an exogenous rate $\delta$ so the steady state conditions for type $k$ workers are given by:

$$2m(\theta)\widehat{x}_k u_k = \delta e_k,$$

where $e_k$ is the employment level (or rate) of workers of type $k$. Finally, normalizing the labor force to one implies that:

$$u_B + u_W + e_B + e_W = 1.$$  

(4)

From, (3), (4) and the definition of $p$ we can derive the following steady state relationship:

$$2m(\theta)\widehat{x}_k u_k = \delta (p - u_k),$$

so that:

$$u_B = \frac{\delta (1 - p)}{\delta + 2\widehat{x}_B m(\theta)}, \quad (5)$$

$$u_W = \frac{\delta p}{\delta + 2\widehat{x}_W m(\theta)}, \quad (6)$$
2.2 Asset values of the various labor market states

Contrary to the standard assumption in urban economics where only one employment center prevails (see e.g. Fujita, 1989; Zenou, 2009), here there is a continuum of job locations and jobs are uniformly distributed around the circle. Over their lifetime, workers change jobs but not their residential location so that distance to jobs changes stochastically over time. As a result, on average, over their lifetime, the physical distance to jobs is the same for all workers of type $k$.  

Let $\Omega_k$ be the per-period wealth flow that a worker has access to, either through family funds or through the capital market. We assume that $\Omega_W > \Omega_B$, capturing the idea that black workers have less initial wealth than whites and/or that they have a more difficult access to the capital market. All unemployed workers receive unemployment benefits $b$ (this can also be interpreted as home production) and pay a flow cost $f_k$ of using transportation mode $k$. The cost $f_k$ includes insurance, petrol, lease contract and maintenance for car owners (i.e. $f_W$) and a monthly public transportation card for mass transit users (i.e. $f_B$). Workers can only choose one transportation mode, either for commuting to work (when they are employed) or for job search and shopping (when they are unemployed). So for both car owners and public transport users, the flow cost $f_k$ will be the same independently of their employment status. All workers are risk neutral. Thus, an unemployed worker of type $k$ obtains instantaneous utility $\Omega_k + b - f_k$, while an employed worker, earning $w_k$ and working at a geographical distance $x$, obtains instantaneous utility $\Omega_k + w_k - T_k(x)$, where $T_k(x)$ is total commuting cost at distance $x$. As we will see below, wages do not depend on $x$ because the residential location of each worker is not directly observable.

Let $\tau$ be a positive coefficient and $t_k(x)$ the time it takes to commute to jobs when residing at distance $x$. This implies $\tau w_k t_k(x)$ represents the total time cost for a person residing at

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15 This is why we do not introduce land rent in this model since it would not depend on distance to jobs and will have the same value at each location. Therefore, it will not affect the results of the model.

16 See our discussion at the beginning of Section 2.1.

17 Because it will be shown below that there is a one-to-one correspondence between type and transport mode, subscript $k$ denotes both type and transport mode.
a distance $x$ from her job.\footnote{This is the common way of modelling transport cost in the transport mode choice literature; see for example LeRoy and Sonstelie (1983) and Sasaki (1990). For simplicity and without loss of generality, we have omitted in (7) the variable part of the commuting cost (i.e. the pecuniary commuting cost). Observe however that, in a more general model, the link between commuting costs and the wage paid is achieved through a labor-leisure choice, which implies that a unit of commuting time is valued at the wage rate (see, for example, Fujita, 1989, Chapter 2). However, such a model is cumbersome to analyze, and it is likely not to yield additional insights beyond those available from our simpler approach, which is consistent with the empirical literature that shows that the time cost of commuting increases with the wage (see, e.g. Small, 1992, and Glaeser et al., 2008).} Then, $T_k(x)$ is given by:

$$T_k(x) = f_k + \tau w_k t_k(x)$$

(7)

We show below (in Section 3.4) that, because $\Omega_W > \Omega_B$, there exists an equilibrium where even the most wealthy minority workers (the ones who have been employed most of the time) cannot afford a car while the least wealthy whites (those who have experienced the longest unemployment spells) can. So, from now on, when we talk about transportation issues, $k = B$ implies public transportation while $k = W$ implies cars. As a result, $f_k$ is the pecuniary cost of transportation. We assume that switching transport mode is sufficiently costly so once a transportation mode decision is made, it is always optimal to stick to it even when one becomes unemployed (see Section 3.4). Naturally, we assume that $f_W > f_B$, it is more costly to have a car than to use public transportation. As usual in this type of model, the wage represents the opportunity cost of time. Let $\mu_k$ be the (average) speed of a trip to work for a worker of type $k$. Then,

$$t_k(x) = \frac{x}{\mu_k}.$$  

(8)

We assume that $\mu_W > \mu_B$. Indeed, $\mu_k$ not only measures how fast the transport mode is but also the “smoothness” of the transportation system. As stated in the introduction, it is well-documented that in large U.S. cities, there is a lack of good public transportation.

In this context, distance to jobs can be measured in terms of either physical distance $x$ (i.e. number of miles) or time distance $t_k(x)$ (i.e. hours). In other words, two workers using different transport modes, will not reach the same physical distance during the same time.

Let $U_k$ be the steady-state expected discounted lifetime utility of an unemployed worker\footnote{To save on notation we leave out subscript $i$ when there is no possibility of confusion.} of type $k$ and $E_k(x, w_k)$ be the steady-state expected discounted lifetime utility of an employed worker of type $k$ living at a distance $x$ from her job and earning a wage $w_k$. Then:

$$rU_k = \Omega_k + b - f_k + m(\theta) \left[ 2 \int_0^{\bar{x}_k} [E_k(x, w_k) - U_k] \, dx \right].$$  

(9)
where \( r \in (0, 1) \) is the discount rate, and \( \hat{x}_k \) is the maximum geographical distance a worker is willing to travel (beyond \( \hat{x}_k \) all jobs will be turned down by the unemployed workers). Let us explain this equation. When a worker of type \( k \) is unemployed today, her instantaneous utility is \( \Omega_k + b - f_k \). She then meets vacancies at rate \( m_k(\theta) \) and a fraction \( 2\hat{x}_k \) of the vacancies are located at an acceptable distance from the worker. All jobs beyond distance \( \hat{x}_k \) will be turned down. When a worker accepts a job offer at distance \( x \) from her residential location, she obtains a wealth increase of \( E_k(x, w_k) - U_k \).\(^{20}\) Observe that \( U_k \) does not depend on \( x \) because search is random (i.e. workers just read newspaper advertisements) so firms cannot sort workers by locations.

The asset value for an employed worker who is employed at distance \( x \) from her home is given by:\(^{21}\)

\[
 rE_k(x, w_k) = \Omega_k + w_k \left( 1 - \frac{\tau x}{\mu_k} \right) - f_k - \delta \left[ E_k(x) - U_k \right].
\]

Equation (10) has a standard interpretation. When a worker of type \( k \) is employed today, she works at a distance \( x \) and she obtains an instantaneous net profit of \( y - w_k \). This job can then be destroyed at exogenous rate \( \delta \) and, in that case, the firm loses \( J_k - V \). In (12), a firm with a vacant job pays an instantaneous cost \( \gamma \) to maintain and advertise the vacancy. A contact with a worker occurs at rate \( m(\theta) \) and the firm can either meet a minority worker (with probability \( u_B/(u_B + u_W) \))

\[ rJ_k(w_k) = y - w_k - \delta (J_k - V), \]

\[ rV = -\gamma + \frac{2m(\theta)}{\theta (u_B + u_W)} \left[ u_B \int_0^{\hat{x}_B} (J_B - V) \, dx + u_W \int_0^{\hat{x}_W} (J_W - V) \, dx \right]. \]

Let us explain these two equations. In (11), a firm with a job filled by a worker of type \( k \) obtains an instantaneous net profit of \( y - w_k \). This job can then be destroyed at exogenous rate \( \delta \) and, in that case, the firm loses \( J_k - V \). In (12), a firm with a vacant job pays an instantaneous cost \( \gamma \) to maintain and advertise the vacancy. A contact with a worker occurs at rate \( m(\theta) \) and the firm can either meet a minority worker (with probability \( u_B/(u_B + u_W) \)).

\(^{20}\)The exact mathematical derivation of equation (9) is based on dynamic programming tools (Bellman equations) and can be found in Appendix B in Zenou (2009). The same applies for equations (10), (11), and (12) below.

\(^{21}\)For the model to make sense, we assume throughout that \( \tau < 2\mu_B \) since this guarantees that \( 1 > \tau x/\mu_k \), \( \forall x \in [0, 1/2] \) and \( k \in \{B, W\} \).
who will accept the offer only if the firm is within a geographical distance of $\hat{x}_B$, or meet a white worker (with probability $u_W/(u_B + u_W)$) who will accept the offer only if the firm is within a geographical distance of $\hat{x}_W$. Observe that, according to (11), a workers’ productivity $y$ does not depend on her distance to the jobs, $x$. As a result, all employed workers are, in terms of productivity, identical from the firms’ viewpoint. However, as we will show below, white workers can bargain a higher wage because they have a better outside option due to the fact that $\hat{x}_W > \hat{x}_B$. This implies that firms prefer minority workers over white workers, but still hire white workers because it is more profitable to hire them than to keep a vacant job for one more period.

3 The steady-state equilibrium

A (steady-state) labor market equilibrium consists of labor market tightness, wages, unemployment levels and a maximum traveling distance for minority and white workers $(w^*_B, w^*_W, \hat{x}^*_B, \hat{x}^*_W, u^*_B, u^*_W, \theta^*)$ such that, given the matching technology, all agents (workers and firms) maximize their respective objective function. Labor market tightness is determined by a free-entry condition, wages by Nash bargaining, and maximum traveling distance by an indifference condition between the value of unemployment and the value of employment at the maximum acceptable distance. Finally, unemployment and vacancy levels follow from equilibrium labor market tightness and a steady-state condition on unemployment.

3.1 Labor demand

Firms enter in the labor market up to the point where they make zero (expected) profits, i.e. $V = 0$. Using (11) and (12), we can write:

$$J_k = \frac{y - w_k}{r + \delta},$$

(13)

$$\frac{u_B\hat{x}_B J_B + u_W\hat{x}_W J_W}{u_B + u_W} = \frac{\gamma \theta}{2m(\theta)}.$$  

(14)

Combining (14) and (13) yields

$$\frac{u_B\hat{x}_B (y - w_B) + u_W\hat{x}_W (y - w_W)}{u_B + u_W} = \frac{\gamma \theta (r + \delta)}{2m(\theta)}.$$  

(15)

For given wages $w_B$ and $w_W$, we can derive the direct relationship between $\hat{x}_k$ and $\theta$. By differentiating (15), we obtain:

$$\frac{\partial \theta}{\partial \hat{x}_W} > 0 \quad \frac{\partial \theta}{\partial \hat{x}_B} > 0.$$
This result is quite intuitive. When the area of search increases so that workers are ready to accept jobs located further away, firms create more jobs (or equivalently more firms enter in the labor market) because they have more chance to fill up a vacancy since workers are less “picky”.

3.2 Wage determination

The total intertemporal surplus is shared through a generalized Nash-bargaining process between the firm and the worker. As mentioned before, we assume that firms either do not observe the location of workers or more precisely, their $x$ (the distance between the workers and the firm’s location) or that their location is not verifiable because if a worker living in location $i$ would earn more than the same worker living in location $i'$, workers in location $i'$ would have incentives to report a fake address in location $i$.

As a result, a worker and a firm only bargain over observable factors.\textsuperscript{22,23} Even if firms do not know the exact location of each worker, they know, however, that ethnic minorities use public transportation while whites use cars to commute to their jobs (this will be shown below). In other words, firms do not observe $x$ but they observe $\widehat{x}_B$ and $\widehat{x}_W$. Since traveling time is non-verifiable, it is not part of the wage negotiation. As a result, in the wage bargaining, the value of employment is not given by (10) but by:

$$rE_k^d = \Omega_k + w_k - f_k - \delta [E_k^d - U_k^d],$$

where $U_k^d$, the disagreement payoff for the unemployed worker during bargaining is still given by (9) while $E_k(x, w_k)$ is replaced by $E_k^d(x)$. Hence, during the bargaining process, the actual $x$ does not matter since only the average $x$ per type $k$ is taken into account. This is a standard statistical discrimination argument. The match surplus of workers that is relevant for the wage bargaining is thus $E_k^d - U_k^d$ while the surplus for the firms is: $J_k - V$, which reduces to $J_k$ because of the free entry condition. Nash wage bargaining then implies that:

$$(1 - \beta) [E_k^d - U_k^d] = \beta J_k,$$

where $0 \leq \beta \leq 1$ denotes the bargaining power of workers. In part A of the Appendix, we show that (17) implies:

$$w_k = \frac{(1 - \beta) (r + \delta) b + \beta [r + \delta + 2m(\theta)\widehat{x}_k] y}{r + \delta + 2\beta m(\theta)\widehat{x}_k},$$

\textsuperscript{22}See also Gautier (2002) for a similar approach.

\textsuperscript{23}One could also assume that when a firm and a worker bargain over a wage, it is the average commuting distance of each type of workers that is taken into account. This will not change the main results of this paper but will make the wage a direct function of commuting costs.
For a given $\theta$, wages are increasing in the unemployment benefit $b$, the workers’ productivity $y$, and the workers’ bargaining power $\beta$. More interestingly, for a given $\theta$, by differentiating (18), we have:

$$\frac{\partial w_k}{\partial \tilde{x}_k} = \frac{2(r + \delta) \beta m(\theta)(1 - \beta)(y - b)}{[r + \delta + 2\beta m(\theta)\tilde{x}_k]^2} > 0.$$ (19)

When the area of search $\tilde{x}_k$ increases for type-$k$ workers, they have a better outside option and therefore can bargain higher wages. Since labor-market tightness (i.e. job creation) for minority and white workers is the same and equal to $\theta$, $\tilde{x}_W > \tilde{x}_B$, implies that white workers earn higher wages than ethnic minorities. In other words, by increasing the area of search, car access increases wages. This is a well-documented fact (see e.g. Gurley and Bruce, 2005).

### 3.3 Maximum distance to jobs

We must finally determine the maximum commuting distance a worker is willing to accept, $\tilde{x}_k$. In order to determine $\tilde{x}_k$, we use the asset values of unemployment and employment given by (9) and (10). Formally, $\tilde{x}_k$ is implicitly defined by the home-work distance that makes the worker indifferent between being employed or remaining unemployed:

$$E_k(\tilde{x}_k, w_k) - U_k = 0.$$ (20)

In part B of the Appendix, we show that (20) is equivalent to:

$$\frac{m(\theta)w_k\tau}{\mu_k}\tilde{x}_k^2 + \tau w_k(r + \delta)\tilde{x}_k - (w_k - b)(r + \delta) = 0.$$ (21)

It is easy to verify that there is a unique positive solution to this equation that we denote by $\tilde{x}_k^*$. We show in part B of the Appendix that a condition for both $\tilde{x}_W^* < 1/2$ and $\tilde{x}_B^* < 1/2$ and the net wage to be strictly positive is (33). Note that if $\tilde{x}_k^* \geq 1/2$, for $k = B, W$, then there will be a trivial equilibrium where all workers, whatever their type $k$, accept all job offers. We also show in part B of the Appendix that, for a given $\theta$,

$$\frac{\partial \tilde{x}_k^*}{\partial \mu_k} > 0.$$ (22)

Indeed, when people use a faster transport mode, they also accept jobs involving longer commutes. If whites mainly travel with cars while ethnic minorities use public transportation, then $\tilde{x}_W > \tilde{x}_B$.\(^{24}\)

\(^{24}\)The positive root of $\tilde{x}_k$ is increasing and convex in $w_k$ while, if we consider the relationship between $\tilde{x}_k$ and $w_k$ in (18), we obtain an increasing and concave function in $w_k$. This means that we cannot rule out that
3.4 Transport mode decision

We now derive sufficient conditions for whites to choose cars and blacks to choose public transport. All whites use cars if they can afford it and if no individual white worker reaches a higher utility by using public transport even if firms believe she travels by car. Blacks will always use public transport if they cannot afford a car but can afford to use public transportation.

The highest income that a black worker can obtain is when she is employed forever and perfectly matched to a firm (i.e. $x = 0$). So, no black worker can afford a car if:

$$\Omega_B + w_B < f_W$$  \hspace{1cm} (23)

The worst labor market state for a black worker is unemployment (in that case $x$ does not matter). As a result, blacks can always afford public transport if:

$$\Omega_B + b > f_B$$  \hspace{1cm} (24)

Since we assumed that all workers can use exactly one transport mode, we can rule out that a worker chooses not to invest in transportation and simply collect $b$.

For whites, we need a condition that guarantees that all of them own a car. If the poorest white (who is unemployed) can afford a car, then they all can. So a sufficient condition for all whites to own cars is:

$$\Omega_W + b > f_W$$  \hspace{1cm} (25)

Combining these three conditions gives:

$$f_B - b < \Omega_B < f_W - w_B < f_W - b < \Omega_W$$  \hspace{1cm} (26)

Finally, we need to show that it is not profitable for an individual white worker to switch to public transport even if employers still believe that she has a car. Because employers neither observe car ownership nor residential location, they statistically discriminate workers and base their expectations on aggregate car ownership rates for ethnic minorities and whites.

If sufficiently many whites own a car, then when a firm bargains with a white worker over the wage, it believes that her area of search is $\tilde{x}_W$ and thus offers a wage $w_W$ defined by (18) for $k = W$. Let $\tilde{x}_{W\text{ public}}$ be the maximum acceptable distance for a white worker who
uses public transport. Its value is given by (35) in part C of the Appendix and we show that \( \bar{x}_W^{\text{public}} < \bar{x}_W \) (\( \bar{x}_W \) is given by (21)). In part C of the Appendix, we also show that a necessary and sufficient condition for whites to never deviate and use public transportation is given by:

\[
\left( \bar{x}_W - \bar{x}_W^{\text{public}} \right) \Omega_W + \bar{x}_W (A_I^{\text{car}} - f_W) - \bar{x}_W^{\text{public}} (A_I^{\text{public}} - f_B) > \frac{r (f_W - f_B)}{2m(\theta)}
\] (27)

where \( A_I^{\text{car}} \) and \( A_I^{\text{public}} \) are the average income of a white worker having a car and using public transportation, respectively, and are given by (47) and (48).

To sum up, ethnic minorities will not use cars if \( \Omega_B \) and \( y \) are sufficiently low, implying that our model is only relevant for low-skill workers. Whites own cars if \( \Omega_W \) is sufficiently large. Of course, there exist weaker conditions in which some minority workers own a car and/or some whites use mass transit but, as long as a larger fraction of whites own a car, our results will be qualitatively the same. Finally, if for a small fraction of ethnic minorities, their wealth is equal to that of whites, they may still use mass transit if firms offer them lower wages because the latter believe that all minorities do not own a car.

Observe that the benefit of owning a car is part of the mode choice decision. It is already apparent in condition (26), where the wage of minority workers, i.e. \( w_B \), appears. It is even more apparent in condition (27) where not only the wage but also the unemployment rate of white workers\(^{25}\) are a crucial part of the decision.

As stated in the introduction, the initial wealth difference can also capture the access to the capital market. Assumption (27) implies that if ethnic minorities have a more difficult access to the capital market than whites, then they are more likely to use public transportation. Using US data from the 1992, 1995, 1998, and 2001 waves of the Survey of Consumer Finances (SCF), Charles et al. (2008) show that, not only African Americans pay higher interest rates than whites on the loans used to purchase vehicles, but that they are much more likely to have recently been turned down for a vehicle loan. Another explanation of why African Americans do not have access to a car is that dealers quote lower prices to whites than to them. Indeed, Ayres and Siegelman (1995), who study more than 300 paired audits at new-car dealerships, find that dealers quoted significantly lower prices to white males than to African American males, using identical scripted bargaining strategies. In the context of our model, this would mean that not only \( \Omega_W > \Omega_B \) but that the fixed price of buying a car, \( f_W \), would be much higher for ethnic minorities than for whites. In that case, as compared to whites, the difference between \( \Omega_W \) and \( \Omega_B \) would need to be even less large.

\(^{25}\) which are included in \( A_I^{\text{car}} \) and \( A_I^{\text{public}} \).
for minorities not to be able to buy cars.\textsuperscript{26}

### 3.5 The steady-state equilibrium

**Definition 1** A steady-state equilibrium is a tuple \((w_B^\ast, w_W^\ast, \hat{x}_B^\ast, \hat{x}_W^\ast, u_B^\ast, u_W^\ast, \theta)\) such that equations (18), (21), (5), (6) and (15) are satisfied.

Our main result can be stated as follows (the proof can be found in part D of the Appendix):

**Proposition 1** Assume that (26) and (27) hold. Then, white workers use cars while ethnic minorities take public transportation to commute to their workplace. Consequently, whites will search over a wider area than blacks, i.e. \(\hat{x}_B^\ast < \hat{x}_W^\ast < 1/2\),\textsuperscript{27} earn a higher wage, i.e. \(w_W^\ast > w_B^\ast\), and experience a lower unemployment rate, i.e. \(u_W^\ast < u_B^\ast\).

If there is enough wealth difference between ethnic minorities and whites, then the latter will be able to buy a car while the former will be forced to use public transportation. Because of a slower mode of transportation, ethnic minorities have difficulties to reach jobs located too far away from their residential location and will therefore only accept job offers within their area of residence. On the contrary, white workers will be ready to accept jobs located further away because of their faster and “smoother” transport mode. As a result, whites will spend less time unemployed since more job offers will be acceptable for them and will obtain a higher wage because their bargaining position is better.\textsuperscript{28} The fact that white workers earn higher wages than ethnic minorities (especially African Americans and Hispanics) is well-documented in the United States (see, e.g., Welch, 2003 or Neal, 2006). But this is also true for Europe. For example, for the UK, controlling for individual characteristics and region, Bangladeshis and Pakistanis earn about 40 and 20 percent lower wages than white UK-born (Dustmann et al., 2003).

Note that, in our model, the average distance to jobs (not to acceptable jobs) is the same for minorities and whites and it is equal to 1/4. In the real-world, this is not true; in most US cities, jobs are located relatively far away from where ethnic minorities live (see the spatial mismatch literature exposed in the Introduction and, in particular, the literature overview

\textsuperscript{26}See also Ayres (1991) for similar evidence.

\textsuperscript{27}A condition that guarantees that both \(\hat{x}_W^\ast < 1/2, \hat{x}_B^\ast < 1/2\) and the net wage \(w_k(1 - \tau x/\mu_k)\) to be always strictly positive whatever \(x \in [0, 1/2], k \in \{B, W\}\) is (33), which is given in part B of the Appendix.

\textsuperscript{28}We have run different numerical simulations (that are available upon request) of this model satisfying conditions (26) and (27). We obtain all the results of Proposition 1.
of Ihlanfeldt and Sjoquist, 1998). So if we had started with ex ante inequalities in terms of distance to jobs between ethnic minorities and whites, the differences in outcomes would have even been larger.

To sum-up, our model endogenously shows that, compared to whites, ethnic minorities (i) do not own a car, (ii) experience higher unemployment rates \( u_B^* > u_W^* \) and longer unemployment spells \( 1/[2m(\theta)\hat{x}_B^*] > 1/[2m(\theta)\hat{x}_W^*] \), (iii) earn lower wages \( w_B^* < w_W^* \), (iv) can spend on average more time commuting to work \( (\hat{x}_B^*/(2\mu_B) > \hat{x}_W^*/(2\mu_W)) \), (v) travel on average less miles to go to their jobs \( (\hat{x}_B^*/2 < \hat{x}_W^*/2) \), and (vi) search for jobs over a smaller area \( (\hat{x}_B^* < \hat{x}_W^*) \).

Results (iv) and (v) are surprising and not straightforward but are well-documented features of the spatial labor market of minority and white workers. Indeed, even though minorities are on average further away from jobs, they tend to live closer (in miles) to jobs when they are employed but spend more time traveling. The time cost per mile traveled is thus substantially higher for ethnic minorities than for whites. There is indeed a difference between commuting distance and commuting time. In the United States, in the central city (where a large fraction of African Americans live), travel times are quite long, especially for people who rely on public transportation. For example, in 1995, the average commute distance for workers using private transportation was twelve miles, compared to thirteen miles for those reliant on public transportation. Commute times, however, were more than twice as long on public transit than for those who used private vehicles - twenty two minutes compared to forty-two minutes (Hu and Young, 1999). Results (iv) and (v) are due to the lack of car access among the minority population while the fact that African Americans are on average further away from jobs is often attributed to housing discrimination (Ross and Yinger, 2002; Dymski, 2006) and the willingness to live together (Ihlanfeldt and Scafidi, 2002). In our model, result (iv) is not always true since \( \hat{x}_B^* < \hat{x}_W^* \) and \( \mu_B < \mu_W \). However, if using cars is a much faster transport mode than using public transportation, then this will hold because the first direct effect is stronger than the second indirect effect.

Most empirical studies (both for Europe and the US) have indeed shown that the mean daily commute is lower for whites than for ethnic minorities (see e.g. Patacchini and Zenou, 2005, for the UK, Chung et al. 2001, and Gottlieb and Lentnek, 2001, for the US) while white commuters have longer average commute distances than ethnic minorities (Holzer et al., 1994; Taylor and Ong, 1995). In particular, using the National Longitudinal Survey Youth Cohort (NLSY) for 1981 and 1982, Table 1 from Holzer et al. (1994) displays interesting statistics, which confirm results (i) – (v) and thus Proposition 1.
4 Discussion and policy implications

We have argued that because of wealth differences, whites mainly use cars whereas ethnic minorities use mass transit. The set of feasible jobs in terms of distance is therefore larger for whites. This improves their bargaining position and results in higher wages and lower unemployment rates for whites. Allowing workers to vary their search intensity would only make the differences larger because the returns to search are higher for whites.

All our results are obtained by assuming that firms have no taste for discrimination and that ex ante minorities and whites are located at the same average distance to jobs. It is well-documented that both discrimination (Altonji and Blank, 1999) and distance to jobs (Ihlanfeldt and Sjoquist, 1998) are important factors that negatively affect the labor market outcomes of minority workers. Adding these elements in our model would lead to more pronounced outcomes between blacks and whites.

As in the standard search-matching models (Diamond, 1982; Mortensen and Pissarides, 1999; Pissarides, 2000), there are two types of search externalities: negative intra-group externalities (more job seekers reduce the job-acquisition rate) and positive inter-group externalities (more searching firms increase the job-acquisition rate). In addition, there are intertype search externalities due to the fact that there is some asymmetry in the search process between ethnic minorities and whites. Indeed, white workers exert negative externalities on minority workers because they obtain a job at a faster rate (i.e. $\tilde{x}^*_{W} > \tilde{x}^*_{B}$) and are better paid ($w^*_{W} > w^*_{B}$), which eventually reduces vacancy supply.\footnote{There is a second order positive effect, namely that a higher $\tilde{x}^*_{W}$ has a positive effect on labor market tightness, $\theta$.}

Investments in public transport can have a substantial impact on search activities of low-income workers and thus on their unemployment rate. Indeed, if labor participation for minority workers is affected by poor access to job locations and poor worker mobility, and if public transportation services are designed to effectively link workers with areas of concentrated employment, then increased access to public transit should yield higher levels of employment in particular for African Americans (Sanchez, 1998, 1999; Blumemberg and Manville, 2004).\footnote{Researchers studying the relationship between transportation and employment find that reliable transportation leads to increased access to job opportunity, higher earning, and increased employment stability (Blumemberg, 2000; Cervero et al., 2002; Ong, 2002; Holzer and Ihlanfeldt, 1996).}

Alternatively, programs that help job takers (especially African Americans) obtain a used car - a secured loan for purchase, a leasing scheme, a revolving credit arrangement - may offer real promise and help low-skill workers obtaining a job. This is a standard policy that has
been advocated in the US (see e.g. Pugh, 1998). Stoll (1999) shows that increasing blacks’ and Latinos’ access to cars will lead to greater geographic job search. As in our model, this in turn will lead to higher employment and wages for these groups. Using data from the UK, Patacchini and Zenou (2005) find similar results. They find that, for a given time distance to jobs (measured by the average commuting time of the employed in a given area), unemployed white workers search more intensively than unemployed minority workers. They also show that giving to nonwhite workers the mean level of white (time) distance to jobs and white car access would close the racial gap in search intensity by 50.31 percent. Raphael and Stoll (2001) also found that raising minority car-ownership rates to the white car ownership rate would considerably narrow inter-racial employment rate differentials (see also Raphael and Rice, 2002, Gurley and Bruce, 2005, and Baum, 2009, who found positive effects of car access on employment).31 Also, if one believes that the low rate of car ownership among minority families is driven by discrimination in the automobile insurance and credit markets, then the government should enforce anti-discrimination laws that prevent such behavior.

Some researchers believe that public funds should be spent helping welfare recipients secure cars (Blumenberg and Waller, 2003; O’Regan and Quigley, 1998; Ong, 2002; Waller and Hughes, 1999; Shen, 2001). In the United States, the welfare program allows states to use federal block grants to provide direct purchase assistance for automobiles, to help pay for insurance, and to provide loans for would-be buyers. Ways to Work, a partnership that secures two-year loans for Temporary Assistance for Needy Families (TANF) recipients in twenty-three cities across seventeen states, reported in 2001 that over 85 percent of its loans had gone to vehicle purchase (Goldberg, 2001). Early evaluations of the program show that participants average as much as a 20-percent increase in monthly income once the loan is received.32 One disadvantage of stimulating car use is that average speed is likely to be decreasing in the total number of cars.

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31 Since car ownership and employment are likely to be simultaneously determined, most of these papers either find instruments or use a natural experiment to obtain a casual relationship. For example, Holzer et al. (2003) use an expansion of the San Francisco Bay Area’s heavy rail system to have an exogenous change in the accessibility of inner-city minority communities to a concentrated suburban employment center. On the other hand, Raphael and Stoll (2001) use an instrument variable strategy to overcome the simultaneity problem between car ownership and employment. Gurley and Bruce (2005) convincingly instrument for car ownership and also finds a positive relationship.

32 Tennessee has also recognized the importance of car access for welfare recipients. In addition to a standard vehicle asset exemption amount, their unique benefit program, First Wheels, provides zero-interest loans for the purchase of a used automobile for program participants and for leavers up to twelve months after cash assistance payment end. Gurley and Bruce (2005) show that this program has increased the probability of being employed and leaving welfare.
Our model sheds some light on the policies discussed above. In particular, by providing the exact mechanism by which car ownership affects the labor-market outcomes of minority workers, it helps designing the appropriate policy aiming at improving the outcomes of minority workers.

Although the lack of car ownership among African Americans in the United States contributes to their adverse labor-market outcomes, it cannot explain all of the large gap in unemployment rates between blacks and whites. Since more than 50 percent of jobs are found through friends and relative (see, e.g. Holzer, 1987, 1988), social networks are also an important part of the story (see, e.g. Calvó-Armengol and Jackson, 2004; Calvó-Armengol and Zenou, 2005; Zenou, 2008). We believe that access to cars is related to social networks in the following way. If ethnic minorities are isolated from whites because they live in segregated neighborhoods and have no have access to cars, they will only have access to closed networks of friends, which are limited in obtaining information about possible jobs. Indeed, because of the lack of good public transportation in the US, it is costly (both in terms of time and money) to commute to business centers to meet other types of people (weak ties) who can provide other source of information about jobs (Granovetter, 1973). If ethnic minorities mainly rely on their strong ties (their neighbors who are more likely to also belong to the minority group) and if the latter are mostly unemployed, then there is little chance for them to escape unemployment and find a job.

References


Appendix

A Determination of the wage

The value equation (9) can be written as:

\[ r U^d_k = \Omega_k + b - f_k + m(\theta) \left[ 2 \int_0^{\hat{x}_k} [E_k^d - U_k^d] \, dx \right] \]

\[ = \Omega_k + b - f_k + 2m(\theta)\hat{x}_k \left[ E_k^d - U_k^d \right]. \tag{28} \]

Now, by subtracting (28) from (16), we obtain:

\[ E_k^d - U_k^d = \frac{w_k - b}{r + \delta + 2m(\theta)\hat{x}_k}. \tag{29} \]

Plugging the value of \( E_k^d - U_k^d \) from (29) and of \( J_k \) from (13) into (17) yields

\[ (1 - \beta) \left[ \frac{w_k - b}{r + \delta + 2m(\theta)\hat{x}_k} \right] = \beta \left( \frac{y - w_k}{r + \delta} \right). \]

By manipulating this expression, we obtain (18).

B Determination of the maximum area of search

First, since the value of employment for type \( k \) depends linearly on \( x \), only through traveling time \( \frac{x}{\mu_k} \), we can write

\[ \frac{1}{\hat{x}_k} \int_0^{\hat{x}_k} E_k(x, w_k)dx = \mathbb{E}_x [E_k(x, w_k)|x < \hat{x}_k] = E_k [\mathbb{E}_x(x|x < \hat{x}_k), w_k] = E_k(\hat{x}_k/2), \]

where the last step follows from, \( \mathbb{E}_x(x|x < \hat{x}_k) = \hat{x}_k/2 \). Therefore,

\[ \int_0^{\hat{x}_k} E_k(x, w_k)dx = \hat{x}_k E_k(\hat{x}_k/2). \tag{30} \]

This implies that (9) can be written as:

\[ [r + 2m(\theta)\hat{x}_k] U_k = \Omega_k + b - f_k + 2m(\theta)\hat{x}_k E_k(\hat{x}_k/2). \]

If we evaluate (10) at \( x = \hat{x}_k/2 \), we get:

\[ (r + \delta) E_k(\hat{x}_k/2, w_k) = \Omega_k + w_k \left( 1 - \frac{\hat{x}_k/2}{\mu_k} \right) - f_k + \delta U_k. \]
Combining these two equations leads to: 

\[
rU_k = \frac{(\Omega_k + b - f_k) (r + \delta)}{r + \delta + 2m(\theta)\hat{x}_k} + \frac{2m(\theta)\hat{x}_k}{r + \delta + 2m(\theta)\hat{x}_k} \left[ \Omega_k + w_k \left( 1 - \frac{\tau \hat{x}_k}{\mu_k} \right) - f_k \right] .
\]  

(31)

If we evaluate (10) at \( x = \hat{x}_k \), we get:

\[
(r + \delta) E_k(\hat{x}_k, w_k) = \Omega_k + w_k \left( 1 - \frac{\tau \hat{x}_k}{\mu_k} \right) - f_k + \delta U_k.
\]

Using this last equation, (20) can be written as:

\[
\Omega_k + w_k \left( 1 - \frac{\tau \hat{x}_k}{\mu_k} \right) - f_k = rU_k.
\]

Using the value of \( rU_k \) in (31), this last equation can be written as:

\[
\frac{(\Omega_k + b - f_k) (r + \delta)}{r + \delta + 2m(\theta)\hat{x}_k} + \frac{2m(\theta)\hat{x}_k}{r + \delta + 2m(\theta)\hat{x}_k} \left[ \Omega_k + w_k \left( 1 - \frac{\tau \hat{x}_k}{\mu_k} \right) - f_k \right] = \Omega_k + w_k \left( 1 - \frac{\tau \hat{x}_k}{\mu_k} \right) - f_k,
\]

which is equivalent to:

\[
\frac{m(\theta)w_k \tau}{\mu_k} \hat{x}_k^2 + \frac{\tau w_k (r + \delta)}{\mu_k} \hat{x}_k - (w_k - b) (r + \delta) = 0.
\]

There are two roots in this equation but only one is strictly positive. It is given by:

\[
\hat{x}_k^* = \frac{\tau (r + \delta)}{2m(\theta)\tau} + \frac{\mu_k}{2m(\theta)w_k \tau} \left( \frac{\tau w_k (r + \delta)}{\mu_k} \right)^2 + 4 \frac{m(\theta)w_k \tau (w_k - b) (r + \delta)}{\mu_k}.
\]

Since \( w_k \) is not directly affected by \( \mu_k \) but only indirectly through \( \hat{x}_k \) (see (18)), we have:

\[
\frac{\partial \hat{x}_k}{\partial \mu_k} = \frac{m(\theta)w_k \tau \hat{x}_k^2 + \tau w_k (r + \delta) \hat{x}_k}{2m(\theta)w_k \tau \hat{x}_k \mu_k + \tau w_k (r + \delta) \mu_k} > 0.
\]

Denote

\[
\Phi(\hat{x}_W) = \frac{m(\theta)w_W \tau \hat{x}_W^2}{\mu_W} + \frac{\tau w_W (r + \delta) \hat{x}_W}{\mu_k} - (w_W - b) (r + \delta).
\]

Since \( \hat{x}_W > \hat{x}_B \), for \( \hat{x}_W < 1/2 \) and \( \hat{x}_B < 1/2 \), we must check that

\[
\Phi(1/2) > 0.
\]

which is equivalent to:

\[
\frac{\tau}{2\mu_W} \left( 1 + \frac{m(\theta)}{2(r + \delta)} \right) > 1 - \frac{b}{w_W}.
\]

31
Combining this condition with the one that guarantees that the net wage \( w_k(1 - \tau x/\mu_k) \) is strictly positive, \( \forall x \in [0, 1/2], k \in \{B,W\} \), i.e. \( \tau < 2\mu_B \), we obtain

\[
(1 - \frac{b}{w_W}) \left[ \frac{2(r + \delta)}{2(r + \delta) + m(\theta)} \right] \mu_W < \frac{\tau}{2} < \mu_B,
\]

which is feasible since \( (1 - \frac{b}{w_W}) \left[ \frac{2(r + \delta)}{2(r + \delta) + m(\theta)} \right] < 1 \).

\[\square\]

C Condition for whites to prefer cars

We need to verify that whites always prefer to use a car over public transportation because the net benefits of a car exceed its net cost. Therefore, we define the following steady-state value function of an unemployed white worker having a car:

\[
rU^\text{car}_W = \Omega_W + b - f_W + m(\theta) \left[ 2 \int_0^{\tilde{x}_W} [E^\text{car}_W(x, w_W) - U^\text{car}_W] \, dx \right]
\]

which is (9). Let \( \tilde{x}_W^{\text{public}} \) be the maximum acceptable distance of a white worker who deviates by using mass transit. Observe that this white person will still earn the same wage \( w_W \) as other whites who use cars because firms do not observe transport mode directly and expect that all whites use cars. This is a standard statistical discrimination argument. The values of \( \tilde{x}_W^{\text{public}} \) can be calculated in a similar way as in (21). We obtain:

\[
\frac{m(\theta)w_W\tau}{\mu_B} \left( \tilde{x}_W^{\text{public}} \right)^2 + \frac{\tau w_W (r + \delta)}{\mu_B} \tilde{x}_W^{\text{public}} - (w_W - b) (r + \delta) = 0
\]

Since \( \mu_B \), the speed of the public transportation system, is lower than \( \mu_W \), the speed of cars, and since \( \frac{\partial \tilde{x}_W^{\text{public}}}{\partial \mu_k} > 0 \) (see (22)), it should be clear that \( \tilde{x}_W^{\text{public}} < \tilde{x}_W^\text{car} \equiv \tilde{x}_W^\text{car} \). We can therefore write the steady-state value function of this white worker who deviates by using public transportation as:

\[
rU^\text{public}_W = \Omega_W + b - f_B + m(\theta) \left[ 2 \int_0^{\tilde{x}_W^{\text{public}}} [E^\text{public}_W(x, w_W) - U^\text{public}_W] \, dx \right]
\]

Note that this is the most favorable case for an individual white worker who takes public transport since she has a wage of \( w_W \) but pays the lowest transportation fee \( f_B \). So if this person prefers to have a car rather than using mass transit, then this will guarantee that, in equilibrium, all white workers will own a car. The underlying statistical discrimination mechanism is that employers do not directly observe the transport mode and the location of
each worker but believe that all white workers have a car. The only disadvantage of using public transportation for a white worker who deviates by using mass transit is the smaller set of jobs that is available, i.e. \( \hat{x}_W^{\text{public}} < \hat{x}_W \). The steady-state value functions of an employed white worker who has a car and the one who deviates by using mass transit are respectively given by:

\[
E_{W}^{\text{car}}(x, w_W) = \Omega_W + w_W \left( 1 - \tau \frac{x}{\mu_W} \right) - f_W - \delta \left[ E_{W}^{\text{car}}(x, w_W) - U_{W}^{\text{car}} \right]
\]

\[
E_{W}^{\text{public}}(x, w_W) = \Omega_W + w_W \left( 1 - \tau \frac{x}{\mu_B} \right) - f_B - \delta \left[ E_{W}^{\text{public}}(x, w_W) - U_{W}^{\text{public}} \right]
\]

The condition that guarantees than whites always prefer a car over public transportation can be written as: \( U_{W}^{\text{car}} > U_{W}^{\text{public}} \). Since \( U_{W}^{\text{car}} \) and \( U_{W}^{\text{public}} \) do not depend on \( x \), equation (34) and (36) can be written as:

\[
[r + 2m(\theta)\hat{x}_W] U_{W}^{\text{car}} = \Omega_W + b - f_W + 2m(\theta) \int_0^{\hat{x}_W} E_{W}^{\text{car}}(x, w_W)dx
\]

\[
[r + 2m(\theta)\hat{x}_W]^{\text{public}} U_{W}^{\text{public}} = \Omega_W + b - f_B + 2m(\theta) \int_0^{\hat{x}_W} E_{W}^{\text{public}}(x, w_W)dx
\]

Given than \( \hat{x}_W > \hat{x}_W^{\text{public}} \) (whites know that if they have a car, then \( \hat{x}_W > \hat{x}_W^{\text{public}} \)), we have: \( r + 2m(\theta)\hat{x}_W > r + 2m(\theta)\hat{x}_W^{\text{public}} \). As a result, using (39) and (40), the condition \( U_{W}^{\text{car}} > U_{W}^{\text{public}} \) can be written as:

\[
2m(\theta) \left[ \int_0^{\hat{x}_W} E_{W}^{\text{car}}(x, w_W)dx - \int_0^{\hat{x}_W} E_{W}^{\text{public}}(x, w_W)dx \right] > f_W - f_B
\]

Using a similar argument as in (30), we can write

\[
\int_0^{\hat{x}_k} E_k(x, w_k)dx = \hat{x}_k E_k(\hat{x}_k/2)
\]

which we use to write (39) and (40) as:

\[
[r + 2m(\theta)\hat{x}_W] U_{W}^{\text{car}} = \Omega_W + b - f_W + 2m(\theta)\hat{x}_W E_{W}^{\text{car}}(\hat{x}_W/2)
\]

\[
[r + 2m(\theta)\hat{x}_W]^{\text{public}} U_{W}^{\text{public}} = \Omega_W + b - f_B + 2m(\theta)\hat{x}_W^{\text{public}} E_{W}^{\text{public}}(\hat{x}_W^{\text{public}}/2)
\]

Equation (42) also implies that (41) can be written as

\[
2m(\theta) \left[ \hat{x}_W E_{W}^{\text{car}}(\hat{x}_W/2) - \hat{x}_W^{\text{public}} E_{W}^{\text{public}}(\hat{x}_W^{\text{public}}/2) \right] > f_W - f_B
\]
If we now evaluate \( E^\text{car}_W(x, w_W) \) and \( E^\text{public}_W(x, w_W) \), defined by (37) and (38), at \( x = \tilde{x}_k/2 \), we obtain:

\[
(r + \delta) E^\text{car}_W(\tilde{x}_W/2, w_W) = \Omega_W + w_W \left( 1 - \frac{\tilde{x}_W/2}{\mu_W} \right) - f_W + \delta U^\text{car}_W
\]

\[
(r + \delta) E^\text{public}_W(\tilde{x}_W/2, w_W) = \Omega_W + w_W \left( 1 - \frac{\tilde{x}_W/2}{\mu_B} \right) - f_B + \delta U^\text{public}_W
\]

Using (43) and (44), these two equations are equivalent to:

\[
r E^\text{car}_W(\tilde{x}_W/2, w_W) = \Omega_W - f_W + \frac{\delta b + \left[ r + 2m(\theta)\tilde{x}_W \right] w_W \left( 1 - \frac{\tilde{x}_W/2}{\mu_W} \right)}{r + \delta + 2m(\theta)\tilde{x}_W} \\

r E^\text{public}_W(\tilde{x}_W/2, w_W) = \Omega_W - f_B + \frac{\delta b + \left[ r + 2m(\theta)\tilde{x}_W \right] w_W \left( 1 - \frac{\tilde{x}_W/2}{\mu_B} \right)}{r + \delta + 2m(\theta)\tilde{x}_W^\text{public}}
\]

Plugging the above two equations into (45) leads to:

\[
\Omega_W \left( \tilde{x}_W - \tilde{x}_W^\text{public} \right) + \tilde{x}_W \left[ \frac{\delta b + w_W \left( 1 - \frac{\tilde{x}_W}{2\mu_W} \right) \left( r + 2m(\theta)\tilde{x}_W \right)}{r + \delta + 2m(\theta)\tilde{x}_W} \right] \\
- \tilde{x}_W^\text{public} \left[ \frac{\delta b + w_W \left( 1 - \frac{\tilde{x}_W^\text{public}}{2\mu_B} \right) \left( r + 2m(\theta)\tilde{x}_W^\text{public} \right)}{r + \delta + 2m(\theta)\tilde{x}_W^\text{public}} \right] \\
> \frac{r (f_W - f_B)}{2m(\theta)} + \tilde{x}_W f_W - \tilde{x}_W^\text{public} f_B
\]

Observe that

\[
u^\text{car}_W = \frac{\delta}{r + \delta + 2m(\theta)\tilde{x}_W}
\]

and

\[
u^\text{public}_W = \frac{\delta}{r + \delta + 2m(\theta)\tilde{x}_W^\text{public}}
\]

are the probabilities to be unemployed for respectively a white who own a car and a white who deviates by using mass transit. Note that \( u^\text{car}_W < u^\text{public}_W \) since \( \tilde{x}_W > \tilde{x}_W^\text{public} \). Therefore, (46) can be written as:

\[
\Omega_W \left( \tilde{x}_W - \tilde{x}_W^\text{public} \right) + \tilde{x}_W \left[ u^\text{car}_W b + (1 - u^\text{car}_W) w_W \left( 1 - \frac{\tilde{x}_W}{2\mu_W} \right) \right] \\
- \tilde{x}_W^\text{public} \left[ u^\text{public}_W b + (1 - u^\text{public}_W) w_W \left( 1 - \frac{\tilde{x}_W^\text{public}}{2\mu_W} \right) \right] \\
> \frac{r (f_W - f_B)}{2m(\theta)} + \tilde{x}_W f_W - \tilde{x}_W^\text{public} f_B.
\]
Denote each average income by:

\[ AI_{W}^{\text{car}} = u_{W}^{\text{car}} b + (1 - u_{W}^{\text{car}}) w_{W} \left( 1 - \frac{\tilde{x}_{W}}{2\mu_{W}} \right) \]  

(47)

and

\[ AI_{W}^{\text{public}} = u_{W}^{\text{public}} b + (1 - u_{W}^{\text{public}}) w_{W} \left( 1 - \frac{\tilde{x}_{W}^{\text{public}}}{2\mu_{W}} \right) \]  

(48)

Using these notations, the inequality above reduces to:

\[ \left( \tilde{x}_{W} - \tilde{x}_{W}^{\text{public}} \right) \Omega_{W} + \tilde{x}_{W} \left( AI_{W}^{\text{car}} - f_{W} \right) - \tilde{x}_{W}^{\text{public}} \left( AI_{W}^{\text{public}} - f_{B} \right) > \frac{r \left( f_{W} - f_{B} \right)}{2m(\theta)} \]

which is (27). Observe that we have shown that: \( U_{W}^{\text{car}} > U_{W}^{\text{public}} \), which, using (41), automatically implies that \( E_{W}^{\text{car}} > E_{W}^{\text{public}} \).

**D Proof of Proposition 1**

Note that \( \frac{\partial e_{k}}{\partial p_{k}} > 0 \) (see (32)). Since whites use a faster transport mode than ethnic minorities, i.e. \( \mu_{W} > \mu_{B} \), this implies that \( \tilde{x}_{W} > \tilde{x}_{B}^{\ast} \). Furthermore, since we have seen that \( \frac{\partial w_{k}}{\partial x_{k}} > 0 \) (see (19)), this implies that \( w_{W} > w_{B}^{\ast} \). Finally, it immediately follows from (5) and (6) that \( u_{W}^{\ast} < u_{B}^{\ast} \).